## EECS 361 Test 2 Topics

- 1) Find the Fourier Transform of aperiodic signals
- 2) Find the Fourier Transform of periodic signals
- Find the Fourier Series of a periodic signal using the relationship between Fourier Transform and Fourier Series

$$x_{P}(t) = \sum_{k=-\infty}^{\infty} x(t - kT_{0}) = \sum_{n=-\infty}^{\infty} x_{n} e^{jn\omega_{0}t}$$
$$x(t) \leftrightarrow X(\omega)$$
$$x_{n} = \frac{1}{T_{0}} X(n\omega_{0})$$

- 4) Apply the Fourier Transform theorems and properties to find  $X(\omega)$
- 5) Find signal power and energy using Parsaval's theorem
- 6) Determine the Transfer Function of linear time invariant systems  $H(\omega) = |H(\omega)| e^{j\theta(\omega)}$ Finding  $H(\omega)$  from block diagram and/or LCCDE
- 7) Determine the output of an LTI system given its input
- 8) Understand the concept of bandwidth and the inverse signal duration/bandwidth relationship
  - First zero definition
    - 3 dB definition
    - Inverse time duration-bandwidth relationship
- 9) Criteria for an ideal linear time invariant system Ideal Filters & Distortionless Transmission
  - a) Distortionless transmission  $y(t)=Kx(t-\tau)$   $H(\omega)=Ke^{-j\omega\tau}$  for all  $\omega$ , i.e.,  $|H(\omega)|=K$  and  $\theta(\omega)=-\omega\tau$ .
  - b) Signal x(t) has bandwidth  $B_{signal}$  then distortionless transmission with respect to x(t) if H( $\omega$ ) has constant amplitude and linear phase (H( $\omega$ )=Ke<sup>-j $\omega\tau$ </sup>) over the signal bandwidth,  $B_{signal}$ .
  - c) ILPF  $\rightarrow$  H( $\omega$ )=Ke<sup>-j $\omega\tau$ </sup> for system bandwidth, B<sub>H</sub>.
  - d) IBPF, IBRF, IHPF
  - e) If B<sub>System</sub>>> B<sub>signal</sub> then negligible distortion, where B<sub>System</sub>=system bandwidth and B<sub>signal</sub>=signal bandwidth
- 16) Basic modulation: DSB-SC, DSB-LC (AM), and FDM: Transmitters and Receivers

## 17) Sampling

- a) Sampling Theorem
- b) Sampling rate  $f_s > 2B$  (Nyquist sampling rate =2B)
- c) Understanding the periodic nature of the spectrum of a sampled signal
- d) Aliasing; causes and remedies
- e) Recovery of x(t) from  $x_s(t)$  using an LPF

18) Discrete Time Signals and Systems

- a) Discrete signal notation, e.g.,  $x[n] = \{a, b, c, d, ...\}$  then x[0] = c
- b) Discrete Time Signals u[n],  $\delta[n]$ ,  $\cos(\Omega n+\phi)$ ,  $\mathbf{p}^n u[n]$

where  $\Omega$ = the discrete-time angular frequency

- c) Discrete time LTI systems
  - Difference equations
  - ARMA format for difference equations
  - Block diagrams with delay blocks
  - Properties of Discrete Time Systems
    - o Linearity
      - Scaling
      - Additivity
    - Time-invariance
    - Memoryless (static) vs Memory (dynamic)
    - BIBO stable
    - o Casual
    - Discrete time impulse response, h[n]
- 19) Discrete Time Convolution
- 20) z-transform
  - a) Finding X(z) given x[n]
  - b) Finding x[n] given X(z)
  - c) Finding transfer function H(z) given
    - The impulse response
    - Difference equation
    - Block diagram
  - d) Finding locations of poles and zeros of H(z)
  - e) Finding frequency response  $H(e^{j\Omega})$  and understanding its relationship to the unit circle.
  - f) Finding the system output given input =  $A\cos(\Omega_{in}n+\phi)$